

**UNIVERSITY OF BOLTON**  
**NATIONAL CENTRE FOR MOTORSPORT**  
**ENGINEERING**  
**BEng (HONS) AUTOMOTIVE PERFORMANCE**  
**ENGINEERING (MOTORSPORT)**  
**SEMESTER 1 EXAMINATION 2023/2024**  
**ENGINEERING MATHEMATICS II**  
**MODULE NUMBER MSP5017**

Date: Wednesday 10<sup>th</sup> January 2024

Time: 14:00 – 16:00

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**INSTRUCTIONS TO**  
**CANDIDATES**

This is an OPEN BOOK examination.

This paper has FIVE questions.  
Answer ALL FIVE questions.

The maximum marks possible for each question and part question are shown in brackets. Note- not all questions carry equal marks.

Electronic calculators may be used if data and program storage memory is cleared prior to the examination.

Mobile phones or tablets may-not be used as calculators.

National Centre of Motorsports Engineering  
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### Question 1

Consider the following equation:

$$x - \cos(2x) = 0$$

- a) Show that the interval  $[0, .1]$  contains a root of this equation. (4 marks)
- b) Use the Newton Raphson method to find this root correct to 5 decimal places. (8 marks)

**Total for Question 1 (12 marks)**

### Question 2

The following Ordinary Differential Equation represents the one quarter model for a car suspension system in the usual notation:

$$m\ddot{x} + c\dot{x} + kx = c\dot{y} + ky \quad (1)$$

In what follows, use values:  $m = 1, c = 2, k = 37, y = t$ .

The General Solution to (1) comprises a complementary function and a particular integral.

- a) Find the complementary function. (8 marks)
- b) Find the particular integral and hence write down the general solution. (8 marks)
- c) If the vertical displacement and velocity are zero at  $t = 0$ , write down the initial conditions, and use these to find the particular solution. (12 marks)

**Total for Question 2 (28 marks)**

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**Question 3**

- a) The Laplace Transform of a function  $f(t)$  is found using the following integral:

$$\mathcal{L}(f(t)) = \int_0^{\infty} f(t)e^{-st} dt$$

Using this definition, find the Laplace Transform of:

i)  $f(t) = e^{2t}$

(4 marks)

ii)  $f(t) = t$

(6 marks)

- b) Use the method of Laplace Transforms to solve the following Ordinary Differential Equation:

$$\dot{x}(t) + 6x(t) = 12e^{6t}$$

given that  $x(0) = 0$ .

(12 marks)

**Total for Question 3 (22 marks)**

**Question 4**

Find and classify the stationary points of the surface defined by:

$$z = 2y^3 - 24y + x^3 - 3x + 27$$

(20 marks)

**Total for Question 4 (20 marks)**

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**Question 5**

For the following double integral:

$$\int_{x=0}^1 \int_{y=-x}^x (x^2 + y^2) dy dx$$

a) Sketch the region of integration.

(5 marks)

b) Evaluate the double integral.

(13 marks)

**Total for Question 5 (18 marks)**

**END OF QUESTIONS**