

**UNIVERSITY OF BOLTON**

**WESTERN INTERNATIONAL COLLEGE FZE**

**BENG (HONS) MECHANICAL ENGINEERING**

**SEMESTER TWO EXAMINATION 2018/2019**

**ENGINEERING PRINCIPLES 1**

**MODULE NO: AME4062**

Date: Thursday 30th May 2019

Time: 10:00 AM – 12:00 PM

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**INSTRUCTIONS TO CANDIDATES:**

There are SIX questions.

Answer Two Questions from Part A  
and Two Questions from Part B.

All questions carry equal marks.

Marks for parts of questions are shown  
in brackets.

Electronic calculators may be used  
provided the data and program storage  
memory is cleaned prior to the  
examination.

**CANDIDATES REQUIRE:**

Formula Sheet (attached)

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**PART A****Q1.**

a) In a mechanical system, deceleration 'a' in  $\text{m/s}^2$ , velocity 'v' in  $\text{m/s}$  and distance 'x' in m, are related by simultaneous equation given below:

$$x + 2v + 3a = -7.8$$

$$2x + 5v - a = 1.4$$

$$5x - v + 7a = 3.5$$

Solve using **determinant method** to find the acceleration, velocity, and distance.

(15 marks)

b) Use Partial fractions to expand:

$$\frac{2x^2 + 7x - 17}{(x-1)(x-2)(x+3)}$$

(10 marks)

**(Total 25 marks)****Q2.**

a) Use partial fractions to expand:  $\frac{8x - 28}{x^2 - 6x + 8}$  (6 marks)

b) The 1<sup>st</sup>, 10<sup>th</sup> and the last terms of an arithmetic progression are 9, 40.5 and 425.5 respectively. Find

i) the number of terms (5 marks)

ii) sum of all terms (3 marks)

iii) the 75<sup>th</sup> term in the series (1 marks)

**Question 2 continued over the page**

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**Q2 Continued.**

b) Forces of  $F_1 = 40\text{N}$  at  $45^\circ$  and  $F_2 = 30\text{N}$  at  $125^\circ$  acting at one starting point. Determine the vector sum ' $\mathbf{F}_1 + \mathbf{F}_2$ ' and vector difference ' $\mathbf{F}_1 - \mathbf{F}_2$ '. Use appropriate figures to represent your answers.

(10 marks)

**(Total 25 mark)****Q3.**

a) If  $x = 3(\cos \pi/4 + j \sin \pi/4)$  find the value of  $x^5$  (5 marks)

b) A drilling machine is to have 6 speeds ranging from 50 rev/min to 750 rev/min. If the speeds form a geometric progression, determine their values, each correct to the nearest whole number. (10 marks)

c) In a system of forces, the relationship between two forces  $F_1$  and  $F_2$  is given

by

$$3F_1 + 2F_2 + 6 = 0$$

$$2F_1 + 4F_2 + 12 = 0$$

Use determinants to solve for  $F_1$  and  $F_2$

(10 marks)

**(Total 25 marks)****Please turn the page**

**PART B**

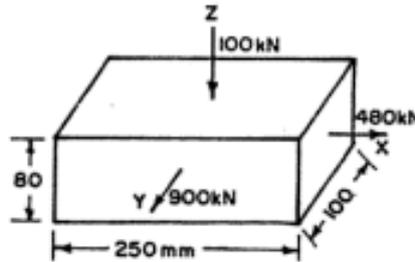
**Q4.**

A rectangular block 250mm x 100mm x 80mm shown in Figure Q4 is subjected to axial loads as follows:

480kN tensile in the direction of its length

100kN compressive on the 250mm x 100mm faces

900kN tensile on 250mm x 80mm faces.



**Figure Q4.** rectangular block

Determine the following:

- Assuming Poisson's ratio as 0.25, find in terms of modulus of elasticity of the material  $E$ , the strains in the direction of each force. (12 marks)
- If modulus of elasticity  $E = 2 \times 10^5 \text{ N/mm}^2$ , find the values of the modulus of rigidity and bulk modulus for the material of the block. (8marks)
- Calculate the change in volume of the block due to loading specified above. (5 marks)

**Total 25 marks**

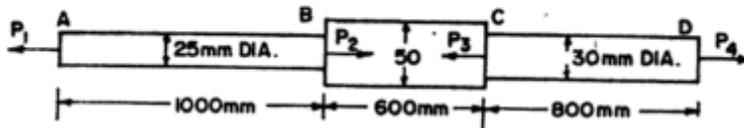
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**Q5.**

- a) A stepped member ABCD is subjected to point loads  $P_1, P_2, P_3$  and  $P_4$  as shown in **Figure Q5a**.

Calculate the force  $P_2$  necessary for equilibrium if  $P_1 = 10\text{kN}$ ,  $P_3 = 40\text{kN}$  and  $P_4 = 16\text{kN}$ . Taking modulus of elasticity as  $2.05 \times 10^5 \text{N/mm}^2$ , determine the total elongation of the member.



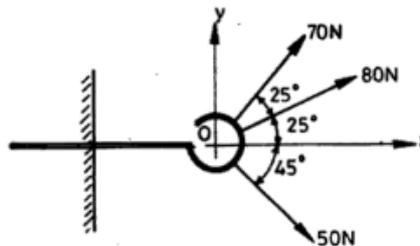
(15 marks)

**Figure Q5a.** stepped member

- b) Three forces are acting on a hook as shown in **Figure Q5b**.

Determine the following:

- I. The resultant force in magnitude (7 marks)
- II. The resultant force in direction (3 marks)

**Figure Q5b.** Forces on a hook**Total 25 marks****Please turn the page**

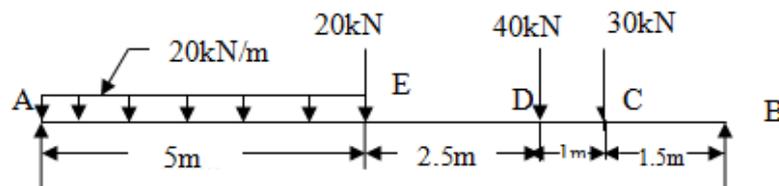
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**Q6.**

A simply supported beam carries concentrated lateral loads at C, D, E and a uniformly distributed lateral load over the length AE as shown in Figure Q6.

Determine:

- i. Reaction loads at the support (5 marks)
- ii. Construct the shear force diagram for the beam (8 marks)
- iii. Construct the bending moment diagram for the beam (8 marks)
- iv. Find the position of maximum bending moment. (4 marks)



**FigQ6.**

**Figure Q6.** Simply supported beam

**Total 25 marks**

**END OF QUESTIONS**

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## **FORMULA SHEET**

### **Determinants**

$$\frac{x}{D_x} = \frac{-y}{D_y} = \frac{z}{D_z} = \frac{-1}{D}$$

### **Matrices**

$$A^{-1} = \frac{adjA}{D}$$

$$X = A^{-1}B$$

### **Series**

$$U_n = a + (n - 1) d$$

$$S_n = \frac{n}{2} [2a + (n - 1) d]$$

$$U_n = ar^{n-1}$$

$$S_n = \frac{a(1 - r^n)}{1 - r}$$

$$S_\infty = \frac{a}{1 - r}$$

$$U_n = a + (n - 1)d + \frac{1}{2} (n - 1)(n - 2)C$$

### **Binomial**

$$(1 + x)^n = 1 + nx + \frac{n(n-1)}{2!} x^2 + \dots$$

$$\text{Validity } |x| < 1$$

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### Partial Fractions

$$\frac{F(x)}{(x+a)(x+b)} = \frac{A}{(x+a)} + \frac{B}{(x+b)}$$

$$\frac{F(x)}{(x+a)(x+b)(x+c)} = \frac{A}{(x+a)} + \frac{B}{(x+b)} + \frac{C}{(x+c)}$$

$$\frac{F(x)}{(x+a)(x^2+b)} = \frac{A}{(x+a)} + \frac{Bx+C}{(x^2+b)}$$

### De Moivre's Theorem

$$(\cos \theta + j \sin \theta)^n = \cos n\theta + j \sin n\theta$$

### Stress

Normal  $\sigma = \frac{P}{A}$  A = x-sectional area

Shear  $\tau = \frac{P}{A}$  A = shear area

### Strain

Normal  $\varepsilon = \frac{\delta l}{l}$

Shear  $\gamma = \frac{x}{y}$  (Angular Displacement in rads in direction of F)

### Compound Bars

$$P = P_1 + P_2$$

$$P = \sigma_1 A_1 + \sigma_2 A_2$$

$$\frac{\sigma_1}{E_1} = \frac{\sigma_2}{E_2}$$

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### Elastic Constants

$$E = \frac{\sigma}{\varepsilon}, \quad G = \frac{\tau}{\gamma}$$

$$\varepsilon_x = \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E} - \nu \frac{\sigma_z}{E}$$

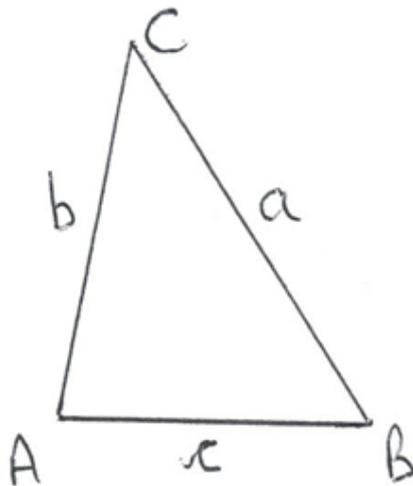
$$\varepsilon_y = \frac{\sigma_y}{E} - \nu \frac{\sigma_x}{E} - \nu \frac{\sigma_z}{E}$$

$$\varepsilon_z = \frac{\sigma_z}{E} - \nu \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E}$$

$$\varepsilon_v = \varepsilon_x + \varepsilon_y + \varepsilon_z$$

$$\varepsilon_v = \frac{1-2\nu}{E} (\sigma_x + \sigma_y + \sigma_z)$$

$$\varepsilon_v = \frac{\delta V}{V}$$



### Compressibility

$$K = \frac{\sigma}{\varepsilon_v}$$

$$\varepsilon_v = \frac{3\sigma(1-2\nu)}{E}$$

$$E = 3K(1-2\nu)$$

$$E = 2G(1+\nu)$$

$$e_v = \frac{\delta L}{L} (1-2\mu)$$

### Trigonometry

Sine Rule:  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine Rule:  $a^2 = b^2 + c^2 - 2bc \cos A$

**END OF FORMULA SHEET**